

# **Radiant Heating Panel Thermal Analysis**

**Prepared by Tim Fleury**

**Harvard Thermal, Inc.**

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*Harvard Thermal, Inc.*  
249 Ayer Road, Suite 102, Harvard, MA 10451  
978-772-3800 • Fax: 978-772-9765  
[www.HarvardThermal.com](http://www.HarvardThermal.com)

## **Analysis Objective**

- Perform a thermal test on a small sample of the concrete panel to determine the Thermal Conductivity and Specific Heat of the concrete
- Generate a thermal model of the panel and heating fluid to determine the heat added to the room per panel
- Document the thermal analysis results



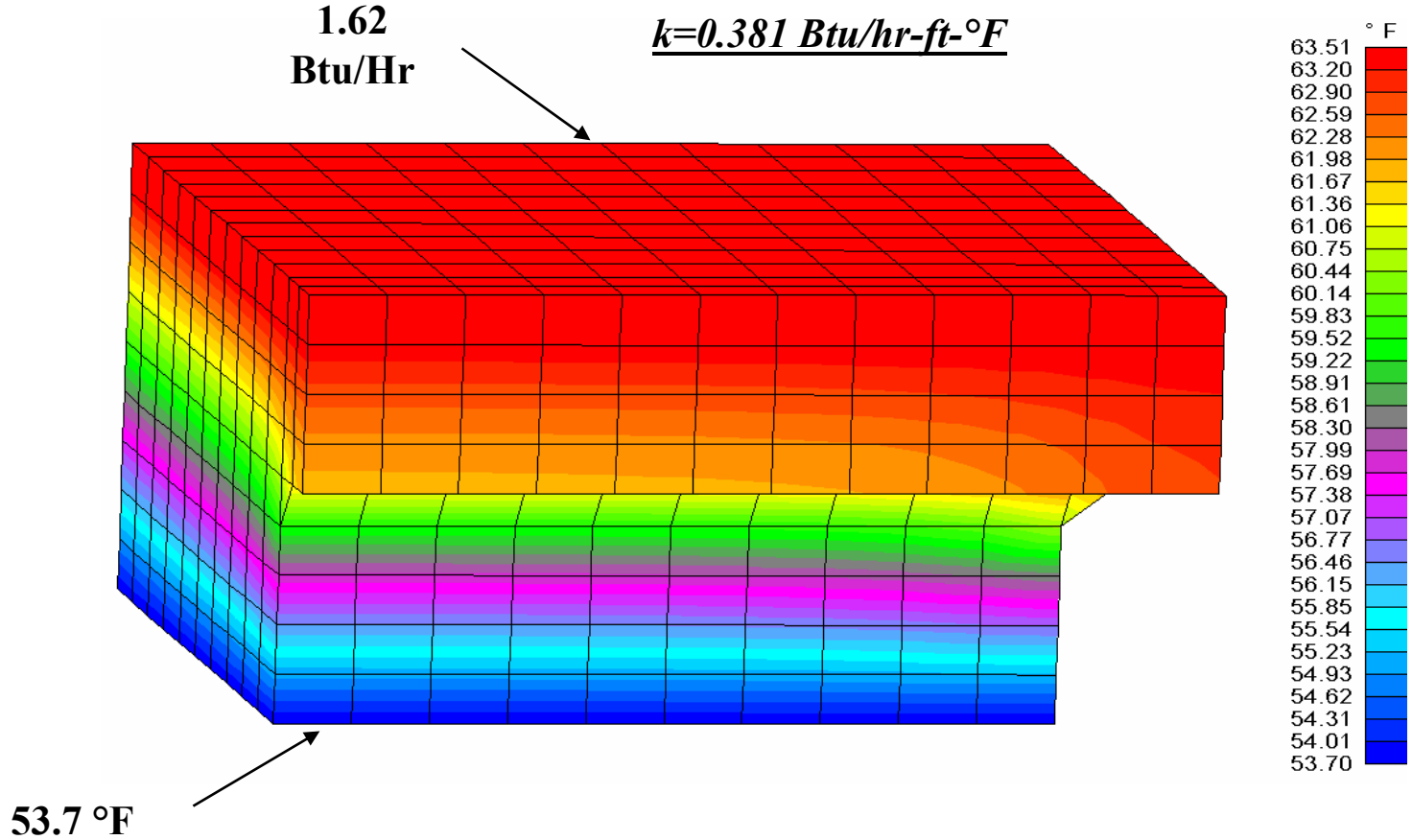
## **Major Assumptions**

- Plastic housing on concrete constructed of Polystyrene or equivalent material with thickness of 0.093 inches
- PEX tubing wall thickness = 0.062 inches
- PEX tubing deforms to fill the groove in the concrete
- Sub flooring consists of ½ inch thick plywood with no insulation
- Room temperature remains constant at 68 °F
- No material on top of concrete
- Radiation emissivity is 0.8 for all surfaces

## **Thermal Conductivity Test - Procedure**

- The purpose of the test was to determine the thermal conductivity of the concrete
- A constant heat load (1.62 Btu/Hr) was applied to one surface of the concrete while the opposite surface was clamped to a coldplate
- Heat load consisted of a resistor attached to a ¼ inch thick aluminum plate
- Thermal grease was used at all interfaces
- The sample was heated to a stabilized temperature of 63.5 °F
- Coldplate was maintained at a constant temperature of 53.7 °F
- A thermal model was generated to verify the test results
- Based on the results, the thermal conductivity of the concrete was calculated to be 0.381 Btu/Hr-ft-°F

# Thermal Conductivity Model

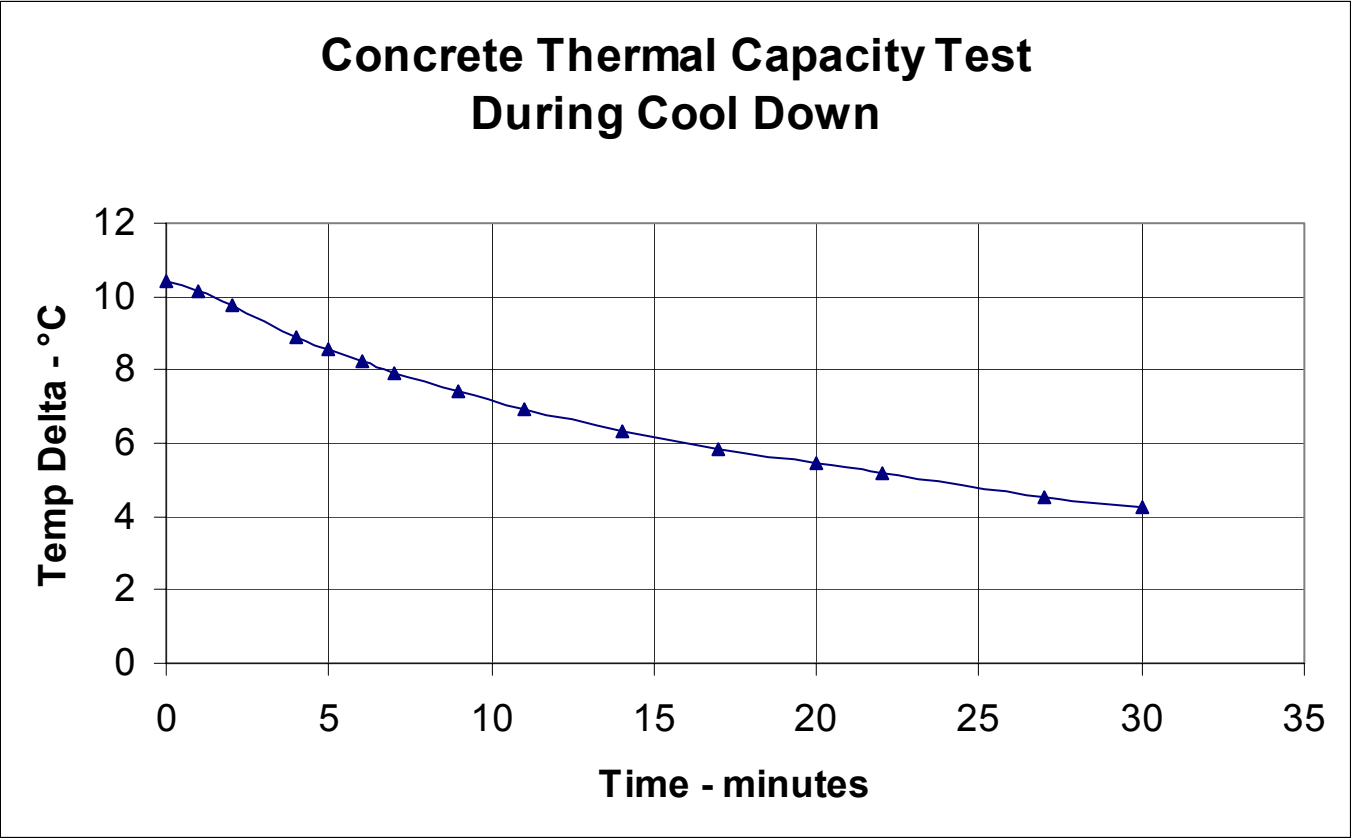


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## **Specific Heat Test - Procedure**

- The purpose of the test was to determine the Specific Heat of the concrete
- Panel sample was heated to a stabilized temperature (63.4 °F) then allowed to cool down with no heat applied
- Coldplate was held to a constant temperature of 53.0 °F
- The heat source was then turned off
- Temperature difference between the heat source area and cold plate interface was monitored during the cool down period
- Based on the results, the Specific Heat ( $C_p$ ) of the concrete was calculated to be 0.19 Btu/lbm-°F

# Specific Heat Test Data



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## Specific Heat Test - Results

- Based on heat transfer formula:

$$(T-T_{cp})/(T_o-T_{cp}) = e^{-t/RC}$$

- At t=30 minutes; T<sub>cp</sub> = 53 °F, T<sub>o</sub> = 63.4 °F, T = 57.3 °F
- Thermal resistance of the sample (extracted from thermal conductivity test) = R = 6.0 Hr-°F / Btu (11.4 °C/W)
- The Capacitance, C, = Specific Heat (Cp) x Weight
- Weight of concrete sample = 0.489 lbs (222 gms)
- Based on the results, the Specific Heat (Cp) of the concrete was calculated to be 0.19 Btu/ lbm-°F

## **Radiant Panel Model**

- A model of the radiant panel was generated using TAS (Thermal Analysis System) software
- Model included the panel, water flow, plywood subfloor, and convection and radiation
- Water inlet conditions were:
  - 0.5 gpm, 90 °F water
  - 0.5 gpm, 140 °F water
  - 2.0 gpm, 90 °F water
  - 2.0 gpm, 140 °F water:

# Material Properties

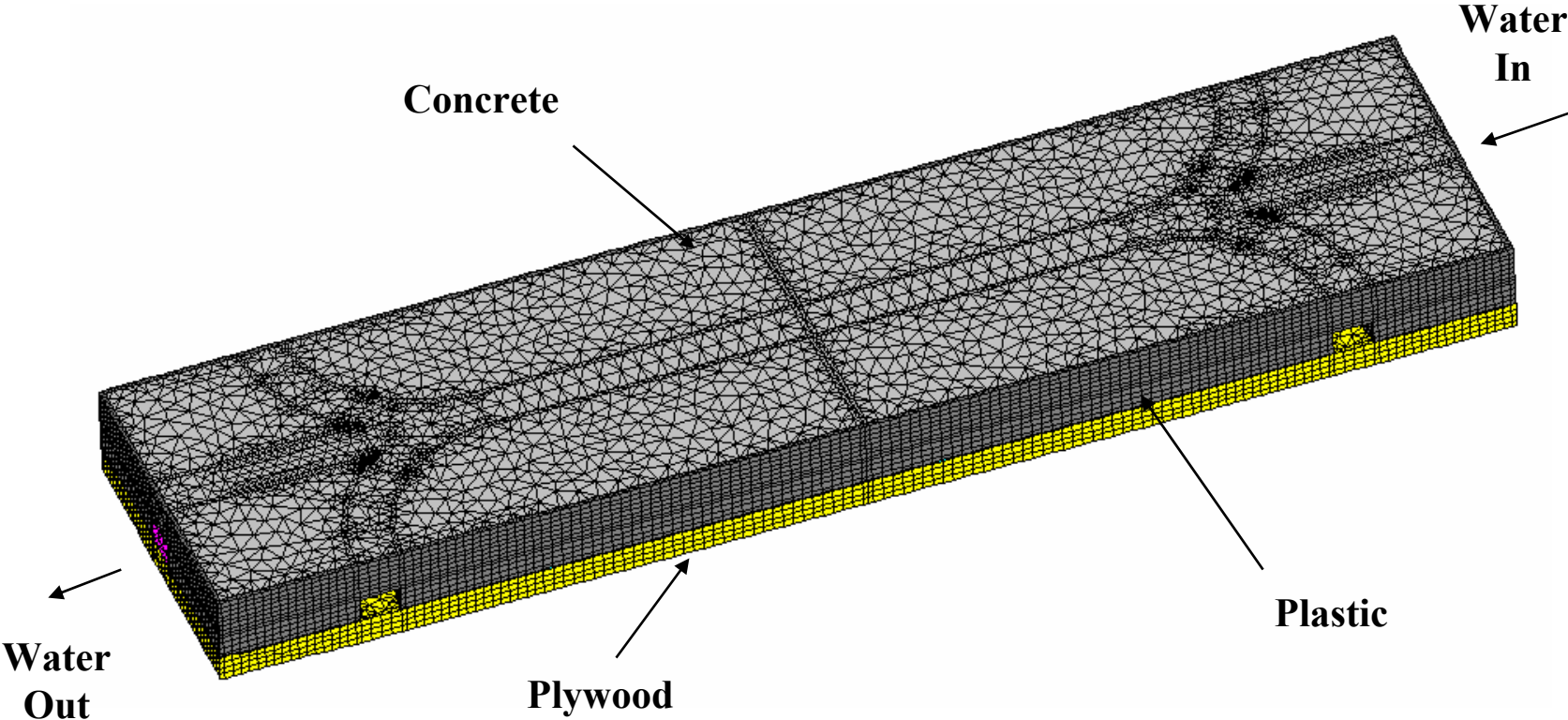
## Thermal Conductivity

Number	1	2	3	4		Units
Description	PEX Tubing	Concrete	Plywood	Polysterene		
X Conductivity	0.018300	0.031750	0.066600	4.580e-003		Btu/(hr-inF)
Y Conductivity	0.018300	0.031750	0.066600	4.580e-003		Btu/(hr-inF)
Z Conductivity	0.018300	0.031750	0.066600	4.580e-003		Btu/(hr-inF)



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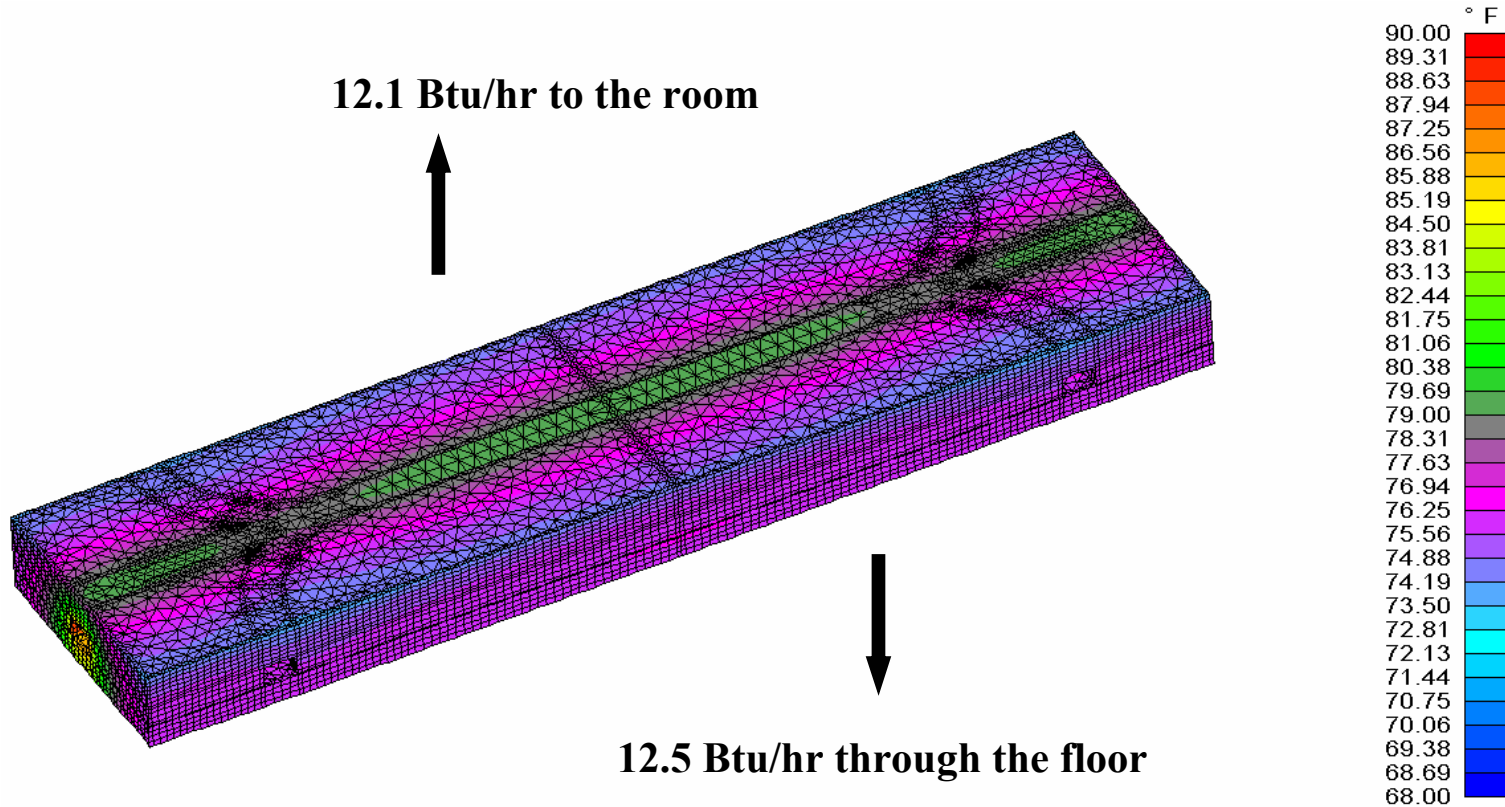
# Radiant Panel Model



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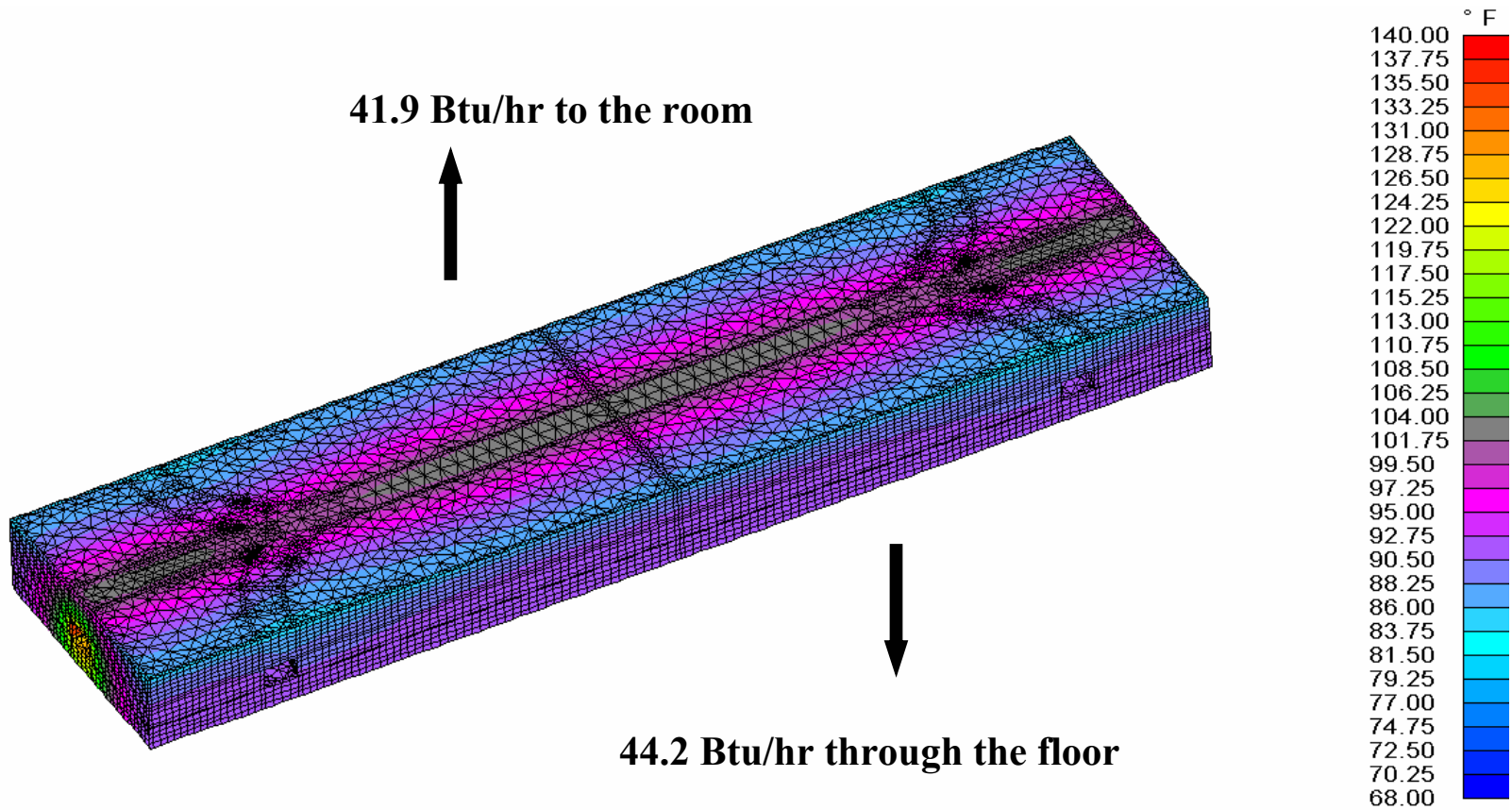
# Thermal Results

## 0.5 GPM, 90 °F



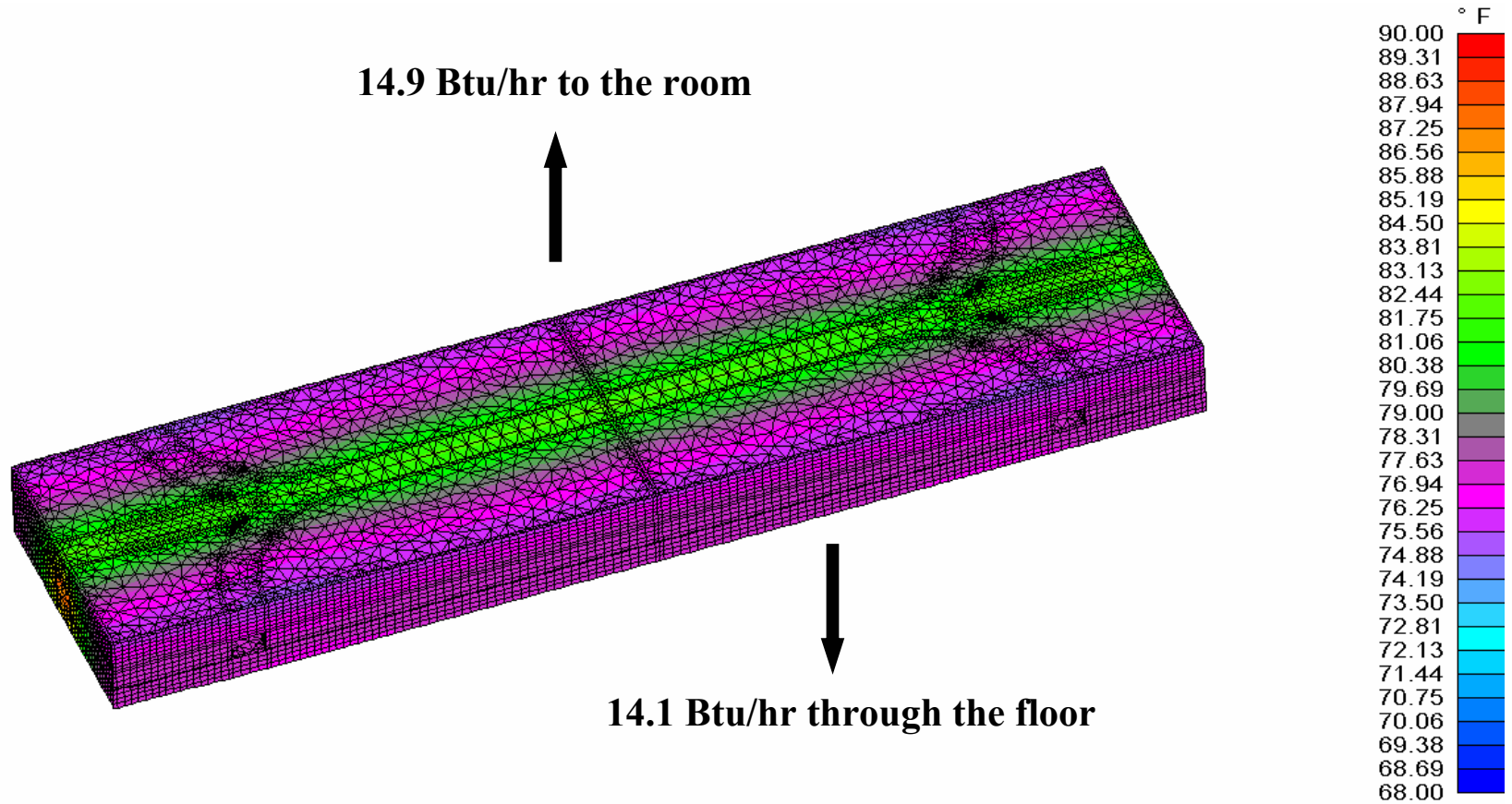
# Thermal Results

## 0.5 GPM, 140 °F



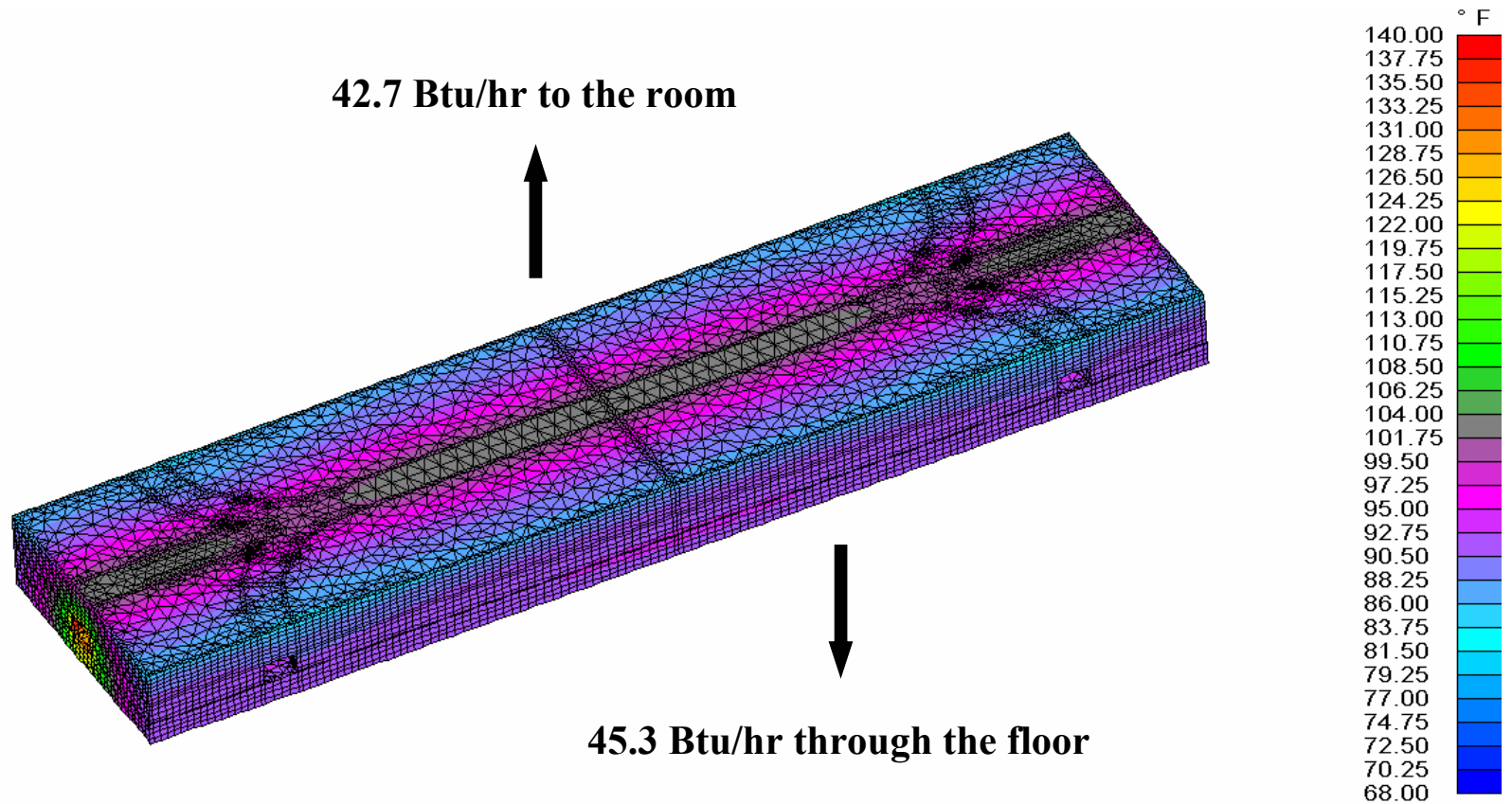
# Thermal Results

## 2.0 GPM, 90 °F

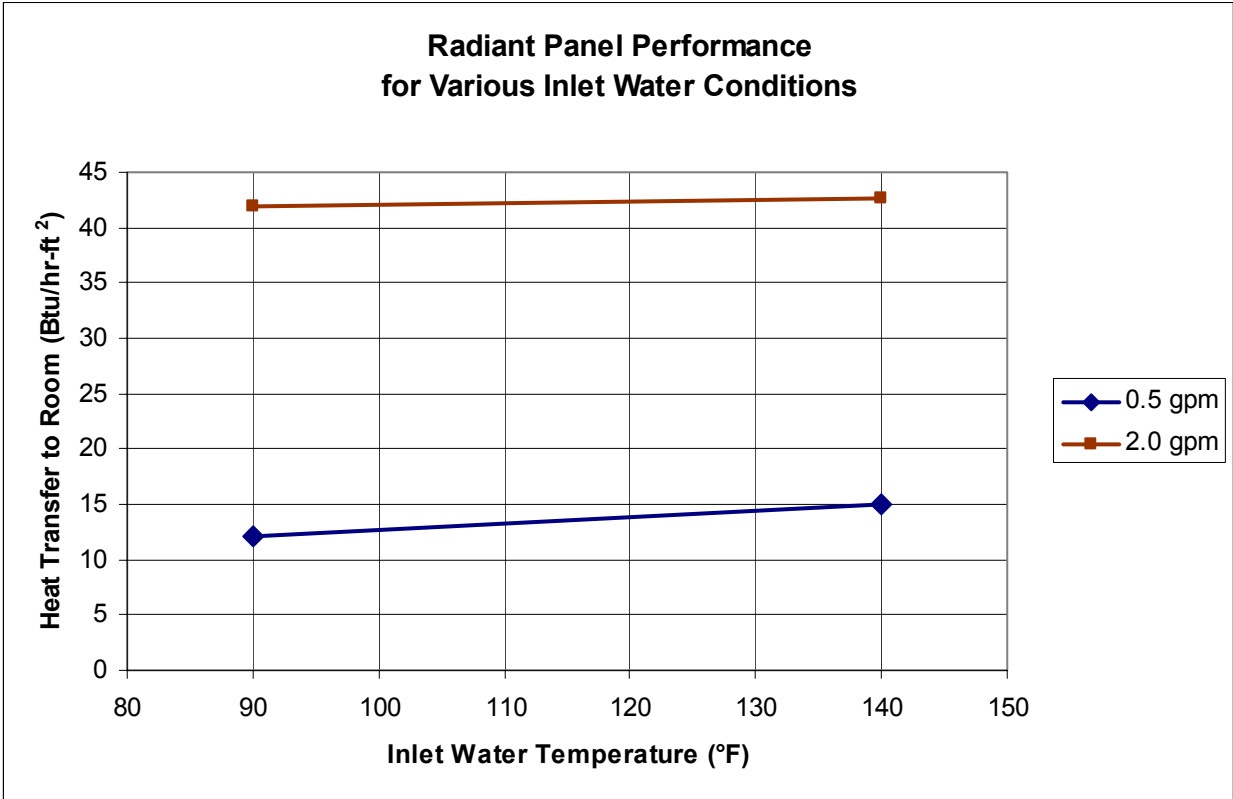


# Thermal Results

## 2.0 GPM, 140 °F



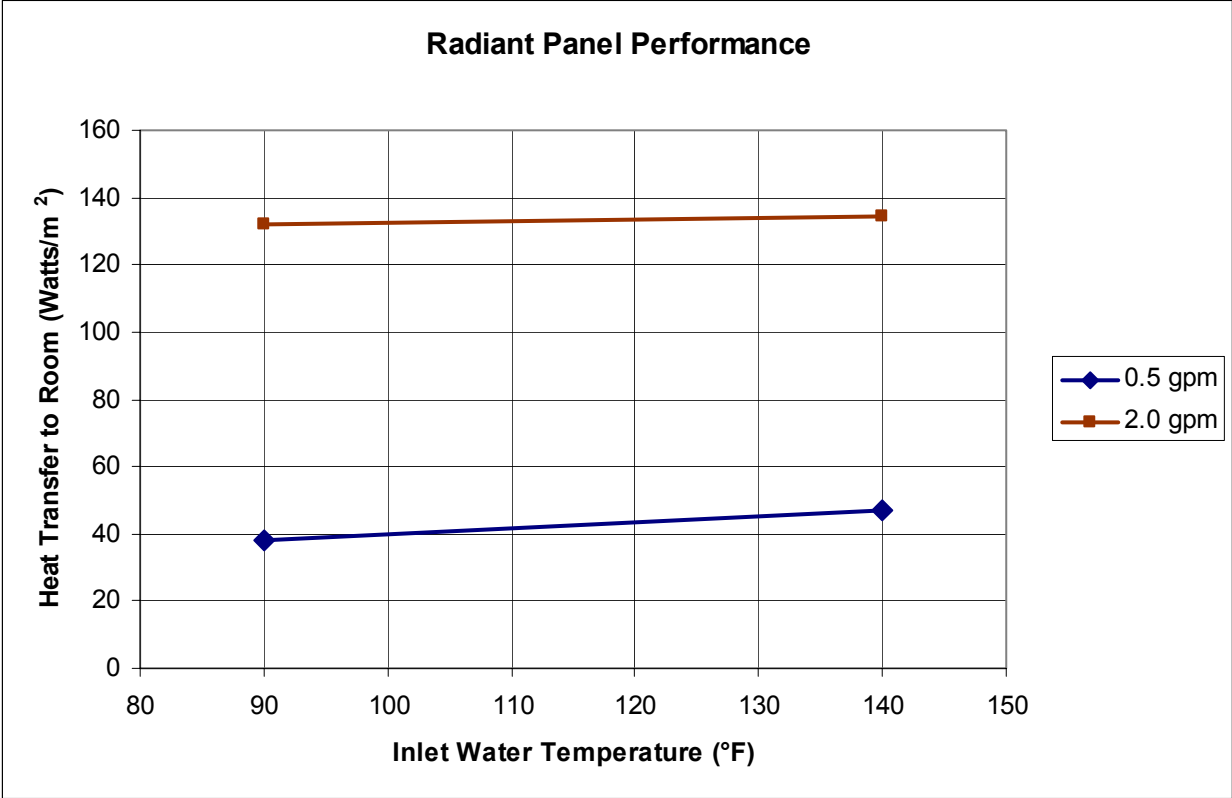
# Radiant Panel Performance Summary



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# Radiant Panel Performance Summary

## SI Units



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## Summary

- The Thermal Conductivity (k) of the concrete was tested to be:

$$k = 0.381 \text{ Btu/hr-ft-}^\circ\text{F}$$

- The Specific Heat (Cp) of the concrete was tested to be:

$$C_p = 0.19 \text{ Btu/lbm-}^\circ\text{F}$$

- The heat transfer rate to the room, per panel, was analyzed to be:

0.5 gpm, 90 °F water: 12.1 Btu/hr-ft<sup>2</sup> (38 W/m<sup>2</sup>)

0.5 gpm, 140 °F water: 41.9 Btu/hr-ft<sup>2</sup> (132 W/m<sup>2</sup>)

2.0 gpm, 90 °F water: 14.9 Btu/hr-ft<sup>2</sup> (47 W/m<sup>2</sup>)

2.0 gpm, 140 °F water: 42.7 Btu/hr-ft<sup>2</sup> (135 W/m<sup>2</sup>)

## Summary (continued)

- The equivalent heat transfer coefficient to the room, per panel, based on a temperature differential between the inlet water temperature and room temperature:

0.5 gpm, 90 °F water: 0.551 Btu/hr-ft<sup>2</sup>-°F (3.13 W/m<sup>2</sup>-°C)

0.5 gpm, 140 °F water: 1.905 Btu/hr-ft<sup>2</sup>-°F (3.30 W/m<sup>2</sup>-°C)

2.0 gpm, 90 °F water: 0.679 Btu/hr-ft<sup>2</sup>-°F (3.85 W/m<sup>2</sup>-°C)

2.0 gpm, 140 °F water: 1.941 Btu/hr-ft<sup>2</sup>-°F (3.37 W/m<sup>2</sup>-°C)

- Half of the heat is transferred through the subfloor
- Adding insulation to the subfloor will improve the heat rate to the room